

## Worksheet #42: Alternating Series Test and The Ratio Test for Absolute Convergence

### Basic Guidelines:

1. The Alternating Series Test for either form  $\sum_{k=1}^{\infty} (-1)^{k+1} a_k$  or  $\sum_{k=1}^{\infty} (-1)^k a_k$  is:

If (a)  $a_k \geq a_{k+1}$  and (b)  $\lim_{k \rightarrow \infty} a_k = 0$ , then the alternating series converges. (If  $\lim_{k \rightarrow \infty} a_k \neq 0$ , then the series diverges.)

2. The Ratio Test for Absolute Convergence: If  $\rho = \lim_{k \rightarrow \infty} \frac{|u_{k+1}|}{|u_k|} < 1$ , then the series  $\sum_{k=1}^{\infty} u_k$  converges absolutely. If  $\rho > 1$ , then the series diverges.

1. Determine whether the following alternating series converge or diverge by the alternating series test:

(a) 
$$\sum_{k=1}^{\infty} (-1)^{k+1} \frac{k}{5k+1}$$

(b) 
$$\sum_{k=1}^{\infty} (-1)^k e^{-2k+1}$$

2. Use the ratio test for absolute convergence to determine whether the series converges or diverges:

(a) 
$$\sum_{k=1}^{\infty} (-1)^k \frac{7^k}{k^3}$$

(b) 
$$\sum_{k=1}^{\infty} (-1)^k \frac{3^k}{k!}$$